

# Psychology 319 – Structural Equation Modeling Course Introduction

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# Psychology 319 – Structural Equation Modeling

## Course Introduction

- 1 Introduction
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## Administrative Details

- Psychology 319, *Advanced Structural Equation Modeling*, is a course that is designed to appeal to students seeking a higher level treatment than our introductory SEM course, Psychology 314, while still remaining accessible to students who haven't taken any course in SEM or are taking a refresher course.

# Administrative Details

- My personal website is at <http://www.statpower.net>. All course readings and information will be posted at the site under the Psychology 319 link.
- Class meetings will be here in Hobbs 107, according to the following schedule:
  - ① 1:10–2:25 Lecture
  - ② 2:25–2:40 Break
  - ③ 2:40–3:45 Lecture
  - ④ 3:45–4:00 Wrap-Up
- Course grading will be based on weekly homework assignments.
- My nominal office hours are T R 11:00-12:00.

## Administrative Details

- You will need R Version 3.0 or later installed on your computers, and you should also install the most recent version of RStudio.
- We will be using the commercial software package, *MPlus 7.1*, in the course to perform analyses. If you do not have a copy of *MPlus* available to you, you can download the free student version from the *Mplus* website.
- We may, for historical reasons, also do a few analyses with *LISREL*, one of the early SEM commercial programs. You can download a free student version of *LISREL* from the SSI website.
- The full version of *MPlus* is running in the Quantitative Lab on the second floor (Hobbs 205). Check and see if you have proxcard access to that room. If you do not, please let me know.

# The Foundation of Structural Equation Modeling

- Structural equation modeling in its modern form can handle an astonishing array of analyses, some of them extraordinarily complex.
- But at its foundation, SEM is based on a very simple idea.

# The Foundation of Structural Equation Modeling

- Think back to your introductory statistics course.
- In the early going, you learned some fundamental rules about the way lists of numbers behave.
- In particular, suppose you have a list of numbers  $X$  equal to 1,2,3.
- This list of numbers has a mean of 2 and a standard deviation of 1.

# The Foundation of Structural Equation Modeling

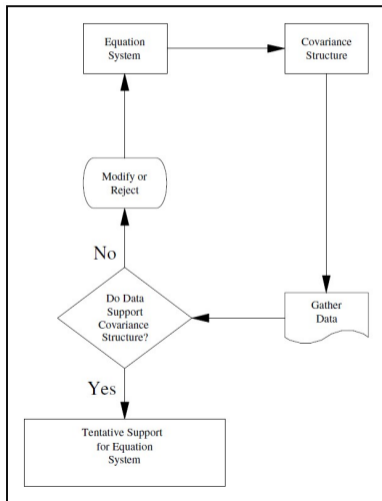
- Now, suppose you were to take these 3 numbers and multiply them by 4. Then the mean would become 8, and the standard deviation would become 4, the variance thus 16.
- *And it would have to be this way.*
- The point is, if you have a set of numbers  $X$  related to another set of numbers  $Y$  by the equation  $Y = 4X$ , then the variance of  $Y$  must be 16 times that of  $X$
- So you can test the *regression model* that  $Y$  and  $X$  are related by the equation  $Y = 4X$  indirectly by comparing the variances of the  $Y$  and  $X$  variables.
- This fact remains true regardless of whether you express the model as a linear equation, or whether you conceive of it in an isomorphic representation known as a *path diagram*.



# The Foundation of Structural Equation Modeling

- This idea generalizes, in various ways, to several variables inter-related by a group of linear equations.
- The rules become more complex, the calculations more difficult, but the basic message remains the same — you can test whether variables are interrelated through a set of linear relationships by examining the variances and covariances of the variables.

# The Foundation of Structural Equation Modeling



# Understanding SEM with Continuous Variables

- The first part of the course deals with the classic models and methods for analyzing path models involving continuous variables.
- A key to understanding how SEM works in the continuous case is to have the skills to derive precisely what *covariance structure* is implied by a particular model.
- In developing the tools to acquire this understanding, we begin by reviewing the key facts about means, variances, covariances, and correlations as developed with scalar algebra in Psychology 310.
- These facts are essential, but scalar algebra is an inefficient medium for manipulating them.
- Matrix algebra, tailored for statistical applications, provides us with a much clearer path to understanding how regression models and covariance structures are related.